

Mining Attribute Evolution Rules in Dynamic Attributed Graphs

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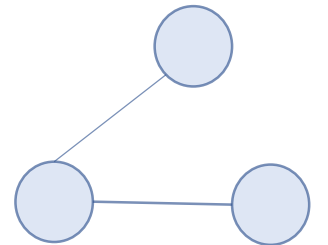
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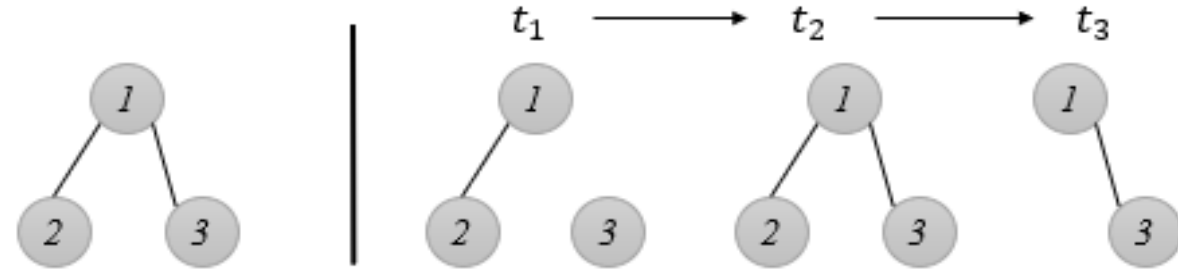
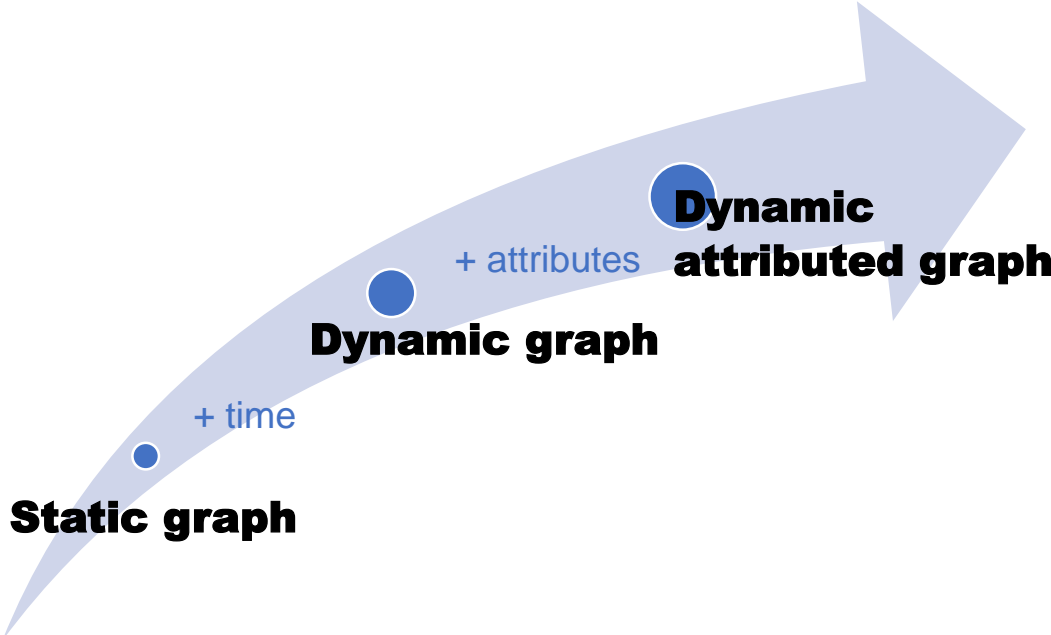
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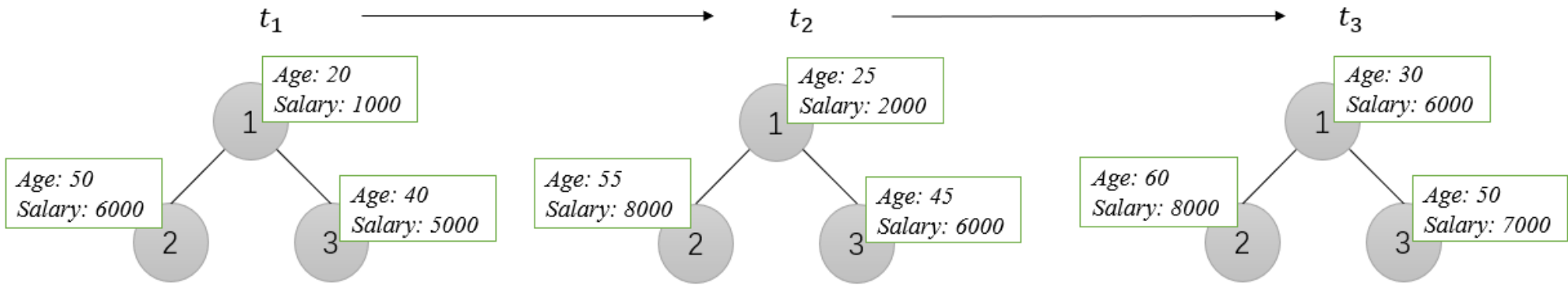


Introduction • What's a dynamic attributed graph?



a) A static graph

b) A dynamic graph



c) A dynamic attributed graph

Introduction • Previous work

1. Pattern mining in dynamic attributed graph

- Cheng et al. (2017) proposed to mining **recurrent pattern** in dynamic attributed graph.
- Desmier et al. (2012) proposed to mining **cohesive co-evolution patterns**.
- Fournier-Viger et al. (2019) proposed to mining **significant trend sequences**.

2. Rule mining in dynamic graph

- Berlingerio et al. (2009) proposed to mining **graph evolution rules**.
- Leung et al. (2010) proposed to mining **interesting link formation rules in social networks**.

Introduction • Limitations

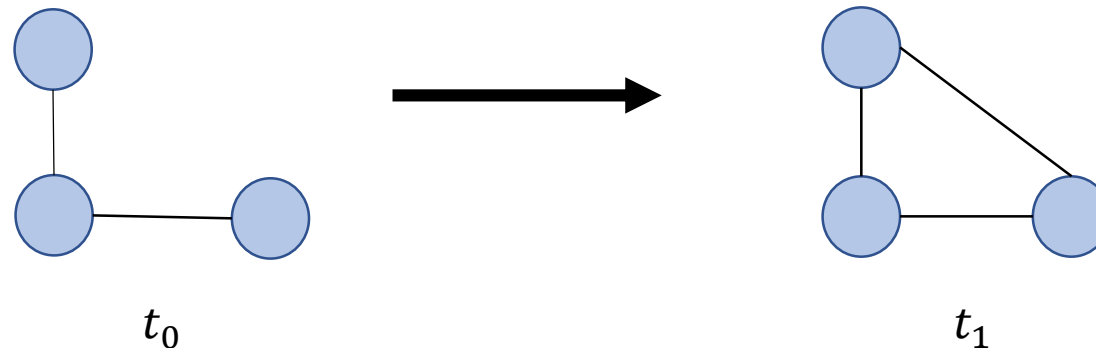
1. Pattern mining in dynamic attributed graph

- All vertices must follow a same trend and may be disconnected (**recurrent pattern**)
- Set of vertices is fixed (**cohesive co-evolution patterns**)
- Focus on influence of a vertex on its neighbors (**significant trend sequences**)

2. Rule mining in dynamic graph

- Only consider topology evolution rather than label evolution.

An example of graph evolution rule

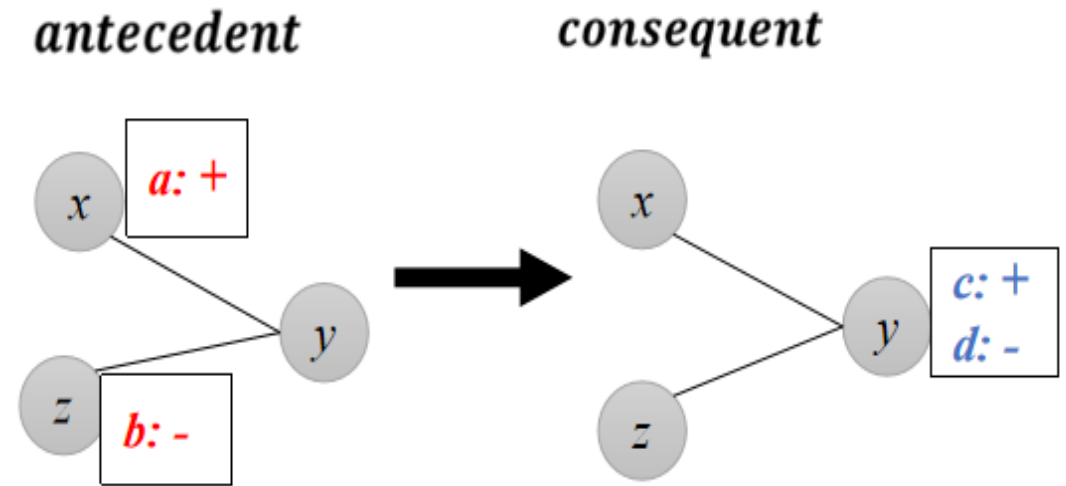


Introduction • Proposal

We propose to mine **attribute evolution rules (AERs)** in dynamic attributed graphs, which focus on finding out evolution rules describing how **attribute values change** for nodes of a subgraph.

Pattern characteristics

- Two parts: antecedent → consequent
- Two consecutive time intervals
- A connected subgraph



An attribute evolution rule

Introduction • Possible usage of AERs

- The **correlation analysis** between attributes in a subgraph.
- **Compression** of graph
- **Prediction** for attributes in nodes of a graph.
- **Recommendation** for next timestamp behavior for social network.
- ...

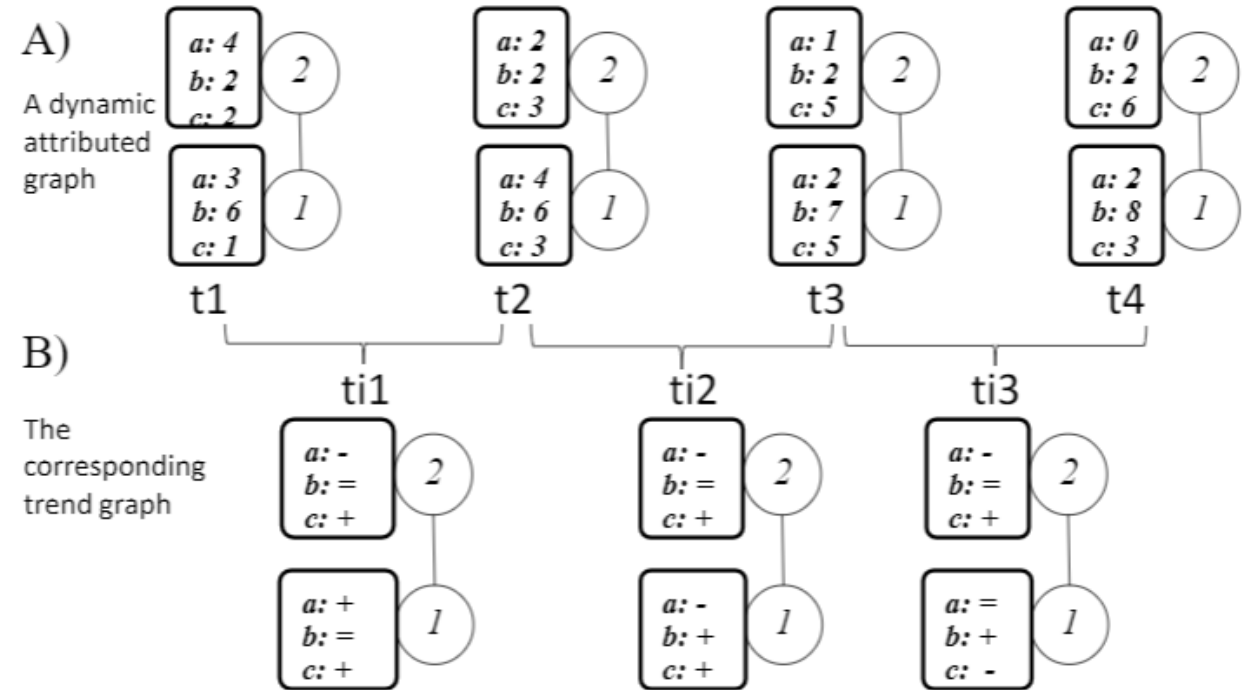
2. Definitions

Definitions

1. Trend graph:

Discretization of continuous attributes for dynamic attributed graph.

The k -th graph G'_k of a trend graph indicates how attribute values have changed in the time interval from timestamp k to $k+1$



2. Attribute evolution rule:

An attribute evolution rule is a tuple $R: (V, E, \lambda_{\text{before}}, \lambda_{\text{after}})$ that indicates how the attribute values of a connected subgraph (V, E) have **evolved** for two consecutive time intervals in a trend graph G' .

Definitions • Measures

Problem: if define the **support** of a pattern as its number of occurrences in **single graph**, the powerful **downward closure property** cannot be directly used to reduce the search space.

Solution:

- maximum independent set-based support (Vanetik 2003).
- MNI (Minimum Node Image) support (Bringmann 2007).
- ...

Definitions • Measure

Our problem can be considered as a **multiple single graphs** sequence. So a modified confidence for is defined **based on MNI**.

An **embedding** of a rule R is a **mapping** between the vertices of the rule and a set of vertices of two consecutive time intervals of a trend graph

c-support:

$$\text{support}(R, G) = \sum_{j=1,2,\dots,max-1} \min_{v \in V_{consequent}} (|embedding(R, G_j)_{j,j+1}|)$$

In short, the least number of **distinct consequent** nodes of its embeddings

Definitions • Correlation measure

C-Confidence: If the antecedent occurs, *how likely* is it will be followed by the consequent.

Lift: The *influence* of the antecedent on the consequent.

$$\text{conf}(R, \mathcal{G}') = \frac{\text{Support}(R, \mathcal{G}')}{\text{Support}(\text{Consequent of } R, \mathcal{G}')}$$

$$\text{lift}(R, \mathcal{G}') = \frac{\text{conf}(R, \mathcal{G}')}{\text{expectedConf}(\text{antecedent of } R, \mathcal{G}')}$$

3. AER-Miner

AER-Miner

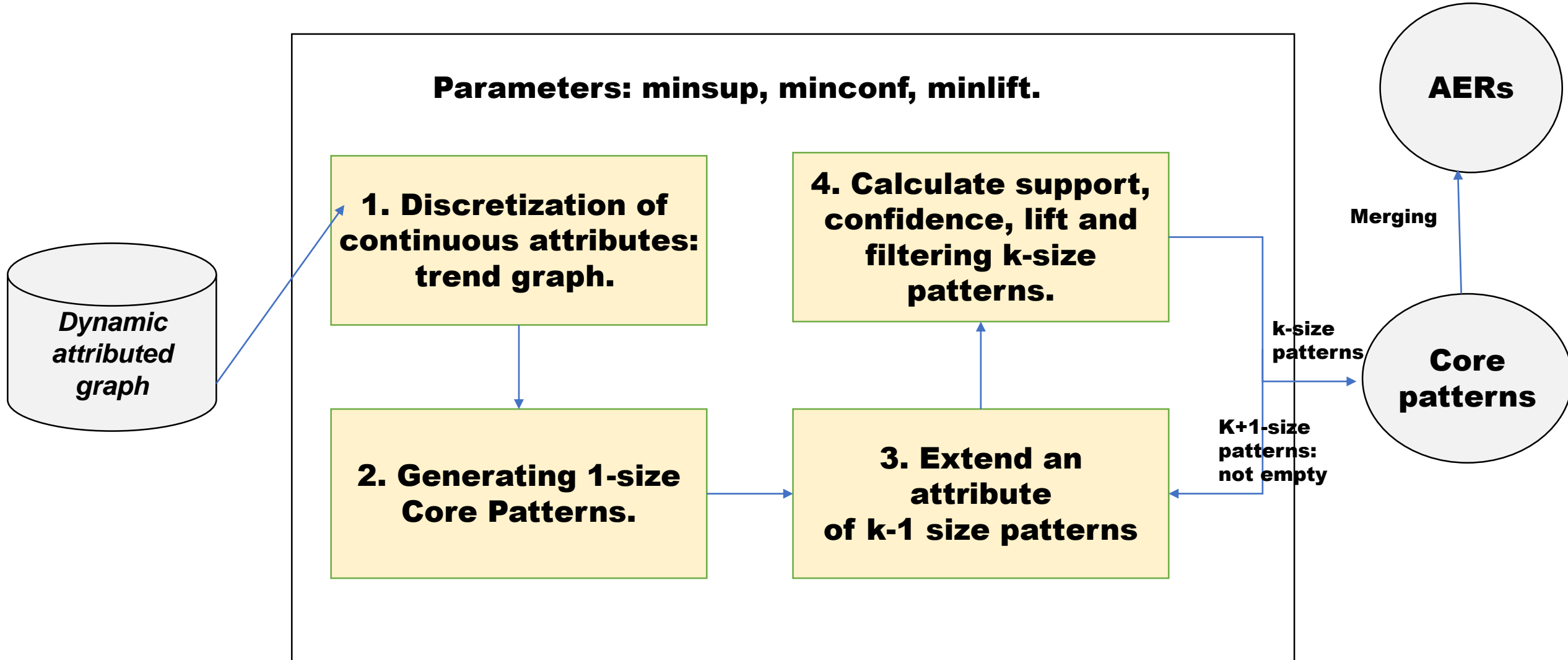
The structure of an AER can be relatively complex. Thus, rather than trying to enumerate all AERs directly, the proposed algorithm first finds **core patterns**, which are a simplified form of AERs. Then, it merges core patterns.

Core pattern:

Core pattern is an AER composed **of a consequent node and several antecedent nodes**, where each consequent-antecedent node pair is **connected**.

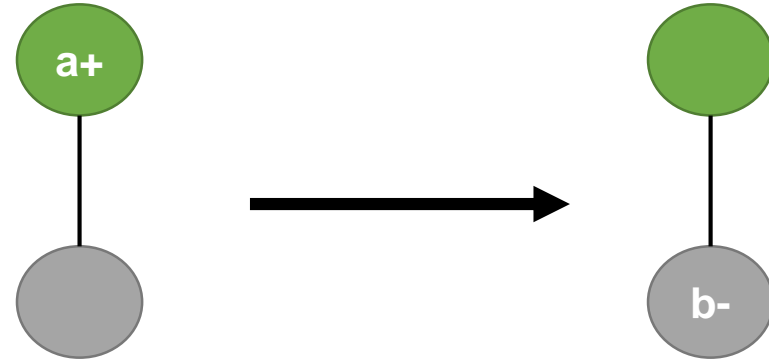
Moreover, each node is described using a **single attribute**.

AER-Miner

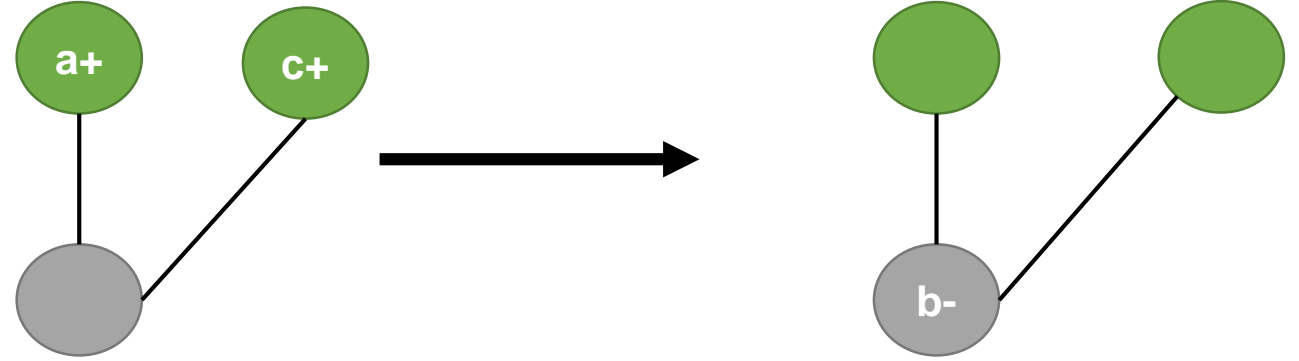


AER-Miner

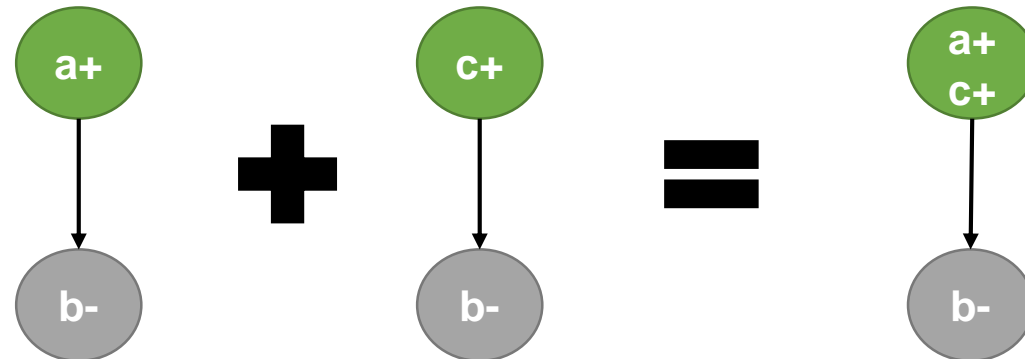
Generating 1-size Core Patterns:



Extend an attribute on k-1 size patterns :



Merging core patterns to AERs:



AER-Miner • Pruning strategies

To reduce search space:

1. **Measures**: support, lift
2. When extending an attribute following a breadth-first search, the attribute order is **lexicographical order**
3. Limit the **size k** of patterns
4. **Ignore** uninteresting attribute trends (e.g. no change)

AER-Miner • Pseudocode

Algorithm 1: The AER-Miner algorithm

input : a dynamic attributed graph \mathcal{G} or trend graph \mathcal{G}' , the *minsup*, *minlift* and *minconf* thresholds
output: all the valid attribute evolution rules

- 1 Initialize a core pattern Map $map_{candidates}$ \langle core pattern,instances \rangle for growing patterns. Initially, each pattern contains one consequent attribute.
- 2 Initialize a list $list_{patterns}$ for storing all possible core patterns.
- 3 while $map_{candidates} \neq \emptyset$ do
 - 4 $map_{k+1sizecandidate} \leftarrow \emptyset$
 - 5 foreach $candidate \in map_{candidates}$ do
 - 6 $pattern \leftarrow candidate.key$
 - 7 $instances \leftarrow candidate.value$
 - 8 foreach $attr \in attributelist$ do
 - 9 if $attr \geq$ the last attribute of pattern and $attr \neq '='$ then
 - 10 $newPattern \leftarrow pattern \cup attr$
 - 11 $newInstances \leftarrow extendInstances(pattern, attr, instaces)$
 - 12 $support \leftarrow sizeofnewInstance$
 - 13 $lift, confidence \leftarrow calLiftAndConfi(pattern, attr, instaces)$
 - 14 if $support \geq minsup$ and $lift \geq minlift$ then
 - 15 | $put \langle newPattern, newInstance \rangle \in map_{k+1sizecandidate}$
 - 16 | end
 - 17 | end
 - 18 | end
 - 19 end
 - 20 $list_{patterns} \leftarrow list_{patterns} \cup map_{k+1sizecandidate}$
 - 21 end
 - 22 $list_{patterns} \leftarrow filterPatterns(list_{patterns}, minconf)$
 - 23 Return $AERs = list_{patterns} \cup mergePatterns(list_{patterns})$

4. Experiment and analysis

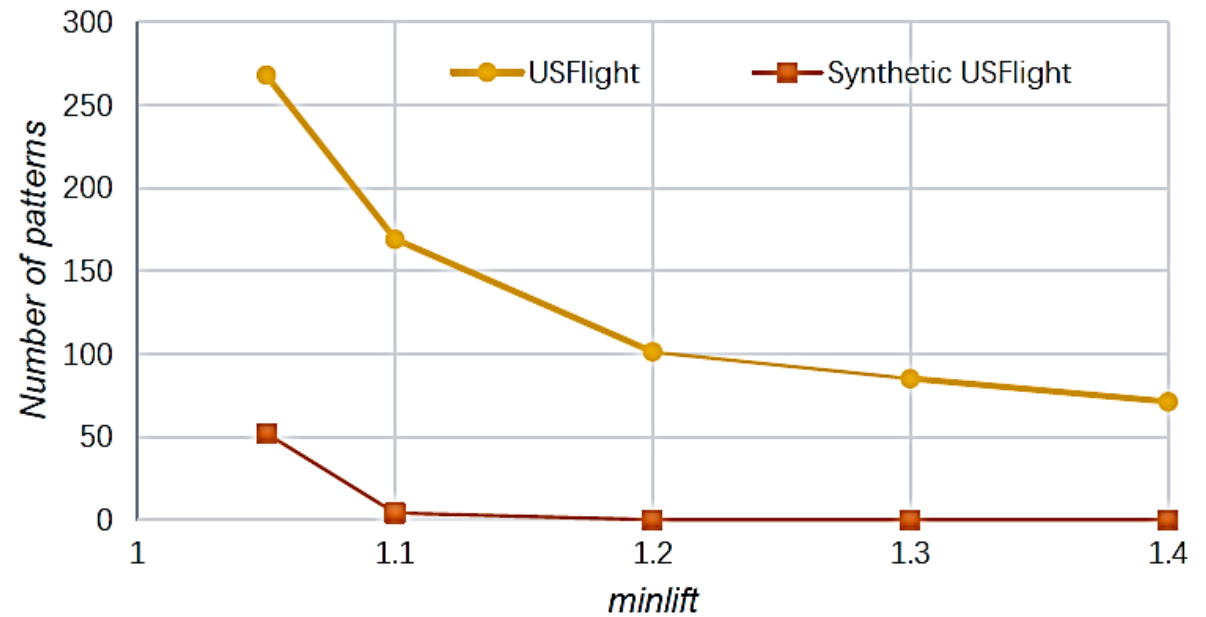
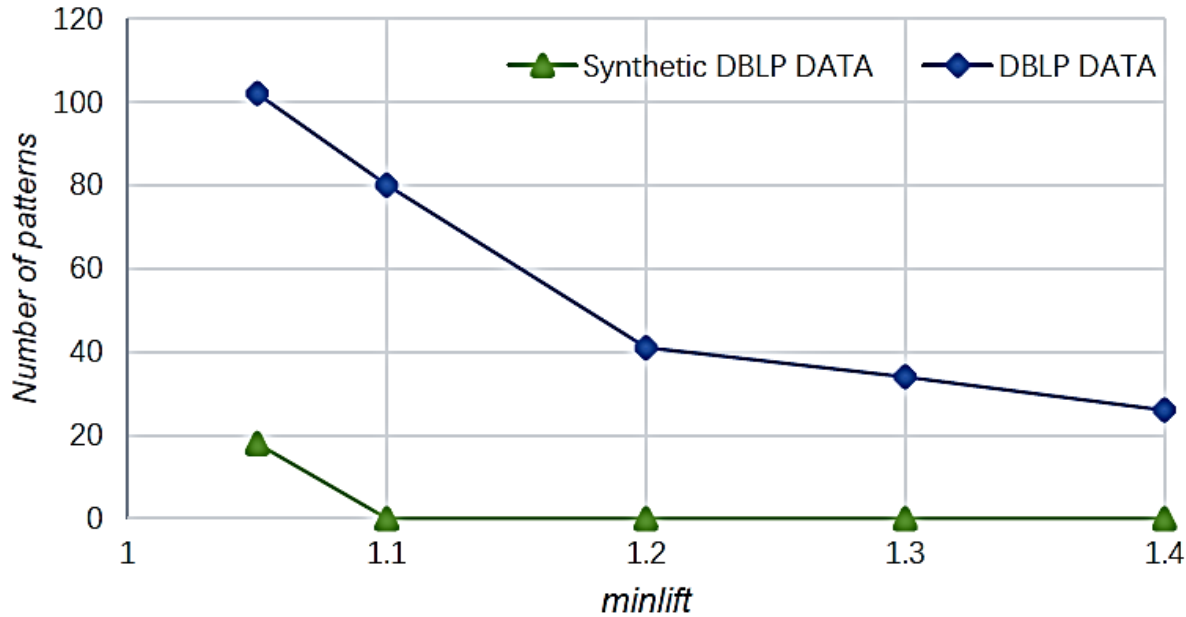
Experiment and analysis

Data

Dataset	Vertices	AvgEdgesPerTimestamp	Timestamps	Attributes
DBLP	2,723	10,737	9	43
US Flight	280	1,206	8	8
synthetic-DBLP	2,723	10,737	9	43
synthetic-USFlight	280	1,206	8	8

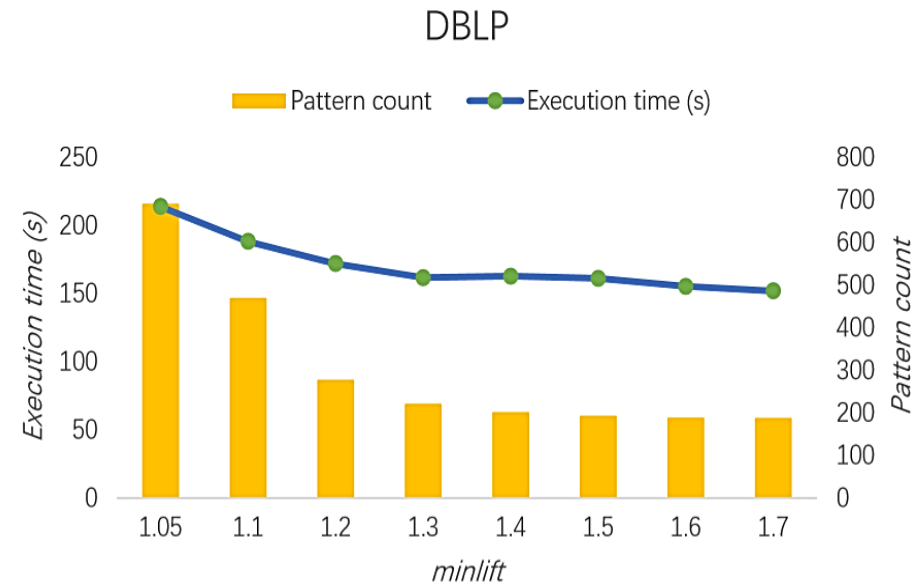
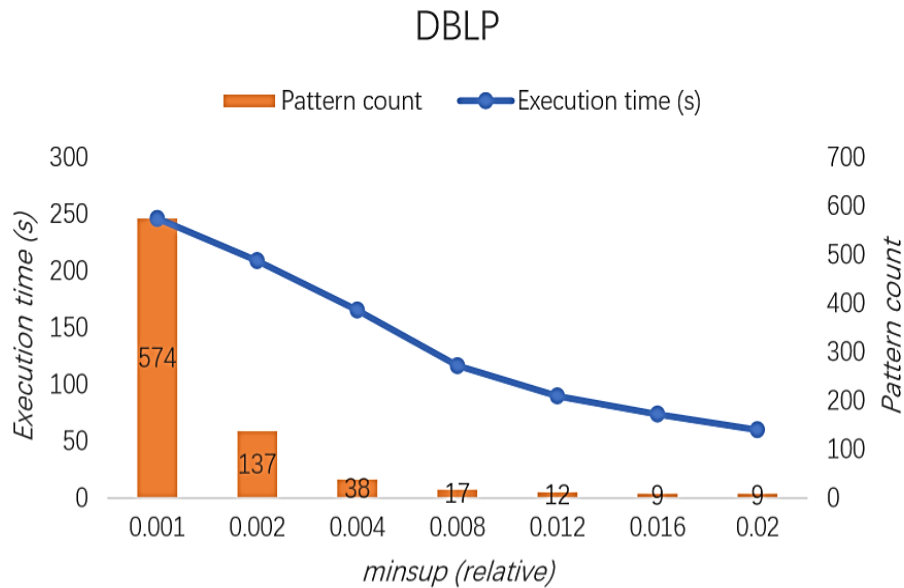
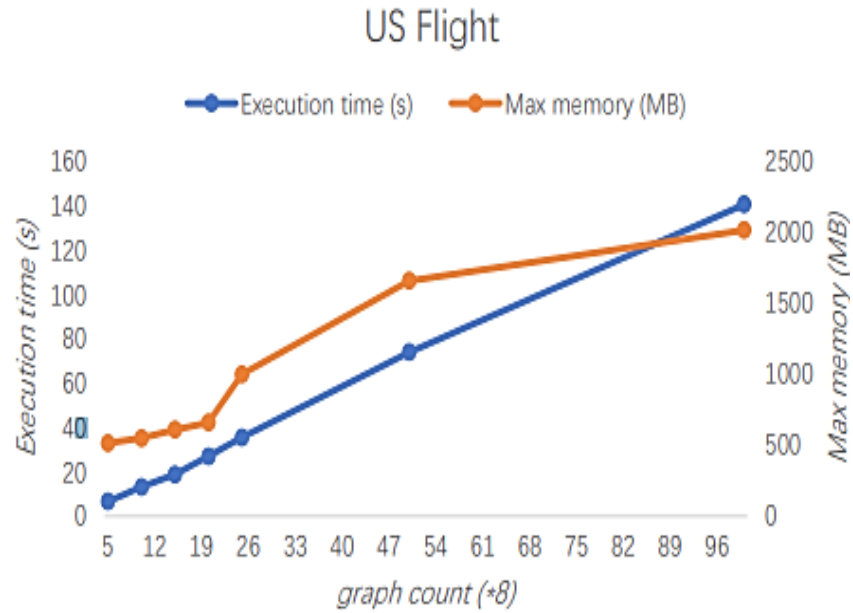
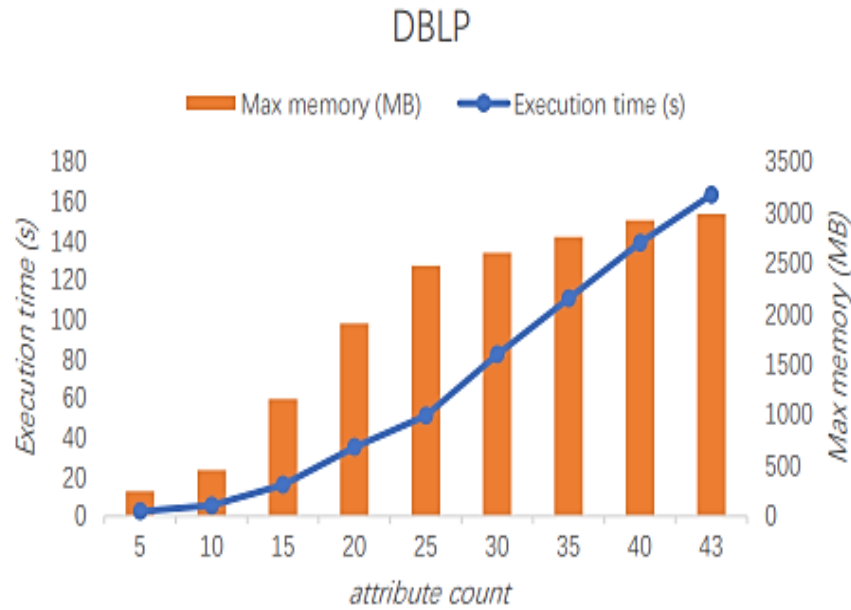
1. **DBLP** is a [co-authorship](#) dataset containing data from the DBLP online bibliographic service.
2. **US Flight** contains data about [US air traffic](#) during the Katrina hurricane period
3. **Two synthetic dataset**: Same topology with above dataset, but [attribute values](#) of each vertex were [randomly generated](#) following a Gaussian distribution.

Statistical validation experiment



- No patterns found for synthetic datasets when *minlift* is large enough
- When *minlift* is small (<1.1), some random or noise AERs also generated in synthetic datasets

Quantitative experiments



Qualitative assessment: interesting real patterns

DBLP

pattern :

$\langle (PVLDB +), (PVLDB +), (PVLDB +) \rangle \rightarrow \langle (VLDB -) \rangle$

US-Flight

pattern:

$\langle (NbDeparture -) \rangle \rightarrow \langle (NbCancellation +) \rangle$

It indicates that departure cancellations caused by the hurricane are strongly correlated with a flight cancellation increase at the next timestamp

5. Conclusion

Conclusion

- Novel type of patterns, **attribute evolution rules**, indicating how changes of attribute values of multiple vertices may **influence** those of others.
- An efficient algorithm named **AER-Miner**.
- **Experiments** on real data have shown that AER-Miner is **efficient** and that AERs can provide **interesting insights** about real-life dynamic attributed graphs.

Q & A



SPMF

Open source Java data mining software, 150 algorithms

<http://www.philippe-fournier-viger.com/spmf/>



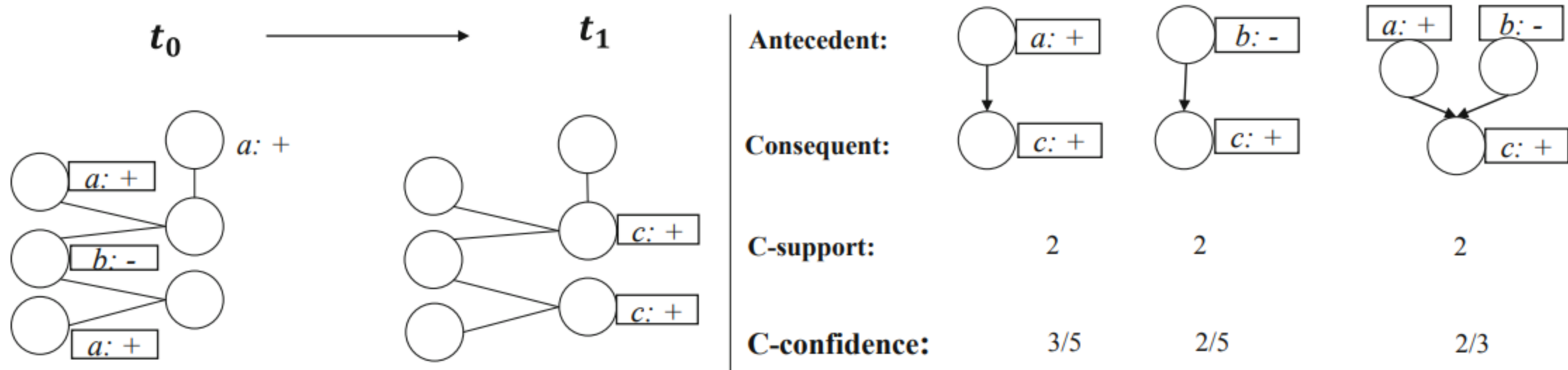


Fig. 3. The c-support and c-confidence of three AERs