

# Mining Partially-Ordered Episode Rules With the Head Support

Philippe Fournier-Viger<sup>1</sup>, Yangming Chen<sup>1</sup>,  
Farid Nouioua<sup>2</sup>, Youxi Wu<sup>3</sup>

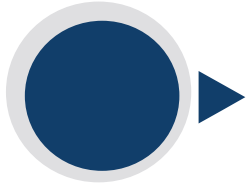
1 Harbin Institute of Technology (Shenzhen), China

2 University of Bordj Bou Arreridj, Algeria

3 Hebei University of Technology, Tianjin, China



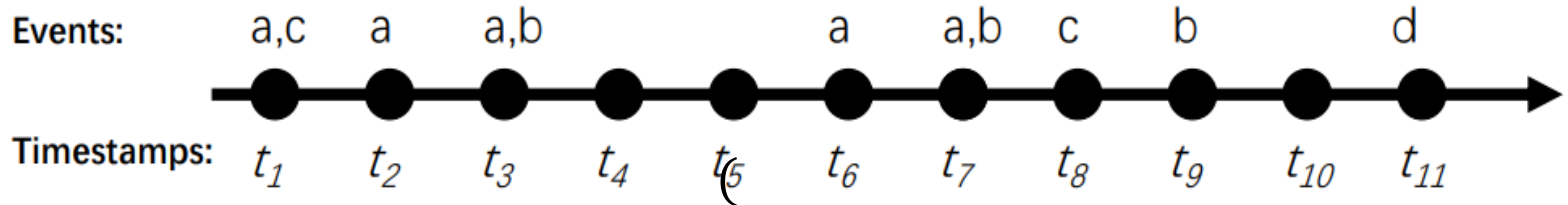
# 1 Introduction



## Frequent Episode Mining

---

**Input:** a sequence of events with timestamps



### Output:

Each frequent episode such that :  
*minimal occurrence count*  $\geq$  *minSup*

### For example:

episode  $\langle \{a,b\}, \{c\} \rangle$

### Episode types:

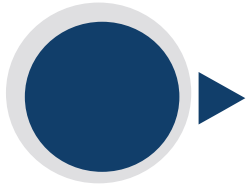
parallel episodes, serial episodes,  
complex episodes

### Algorithms:

WINEPI, MINEPI, EMMA, MINEPI+, ...

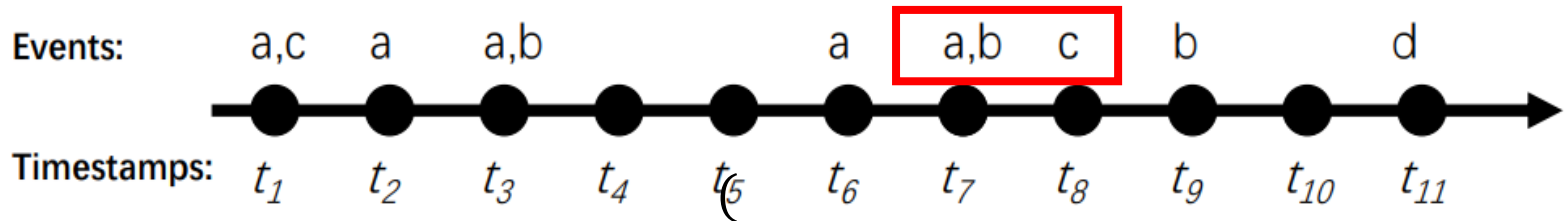


# 1 Introduction



## Frequent Episode Mining

**Input:** a sequence of events with timestamps



### Output:

Each frequent episode such that :  
*minimal occurrence count*  $\geq$  *minSup*

### For example:

episode  $\langle \{a,b\}, \{c\} \rangle$

### Episode types:

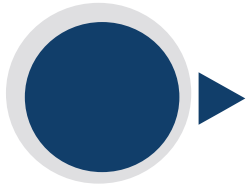
parallel episodes, serial episodes,  
complex episodes

### Algorithms:

WINEPI, MINEPI, EMMA, MINEPI+, ...



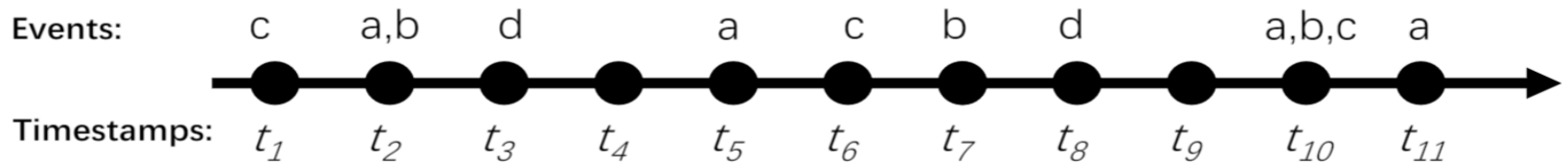
# 1 Introduction



## Episode Rule Mining

---

**Input:** a sequence of events with timestamps



**Output:**

Each episode rule of the form  $X \rightarrow Y$   
such that:

$$(\text{Supp}(X) \geq \text{minSup})$$

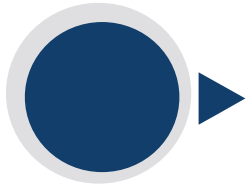
$$(\text{conf}(X \rightarrow Y) = \frac{\text{Supp}(X \cap Y)}{\text{Supp}(X)} \geq \text{minConf})$$

**For example:**

$$\langle \{a\}, \{c\}, \{b\} \rangle \rightarrow \langle \{d\} \rangle$$

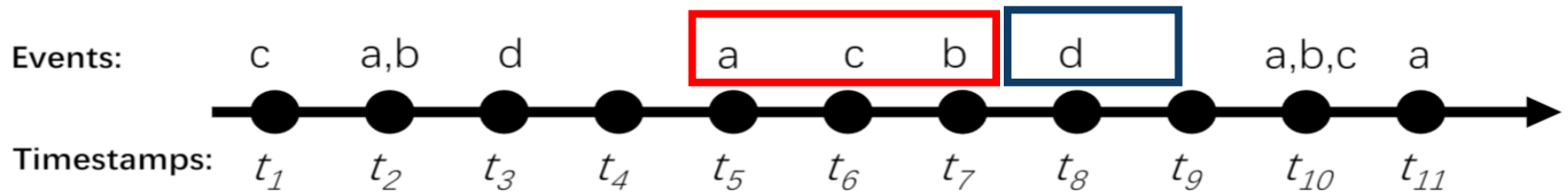


# 1 Introduction



## Episode Rule Mining

**Input:** a sequence of events with timestamps



**Output:**

Each episode rule of the form  $X \rightarrow Y$   
such that:

$$(\text{Supp}(X) \geq \text{minSup})$$

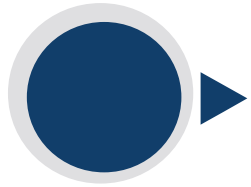
$$(\text{conf}(X \rightarrow Y) = \frac{\text{Supp}(X \cap Y)}{\text{Supp}(X)} \geq \text{minConf})$$

**For example:**

$$\langle \{a\}, \{c\}, \{b\} \rangle \rightarrow \langle \{d\} \rangle$$



# 1 Introduction



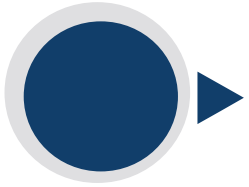
## Previous Work

---

- **Utility-based episode rules**
  - Discovering episodes rule having a high importance in a sequence of discrete events with weights and quantities
- **Precise-Positioning Episode Rules**  
(Ao et al., TKDE 2018, ICDE 2017)
  - the elapsed time between the antecedent and the consequent is fixed
- **Distant and essential episode rules**
  - the antecedent is as small as possible both in terms of number of events and of occurrence duration,
  - consequent is temporally distant from the antecedent.

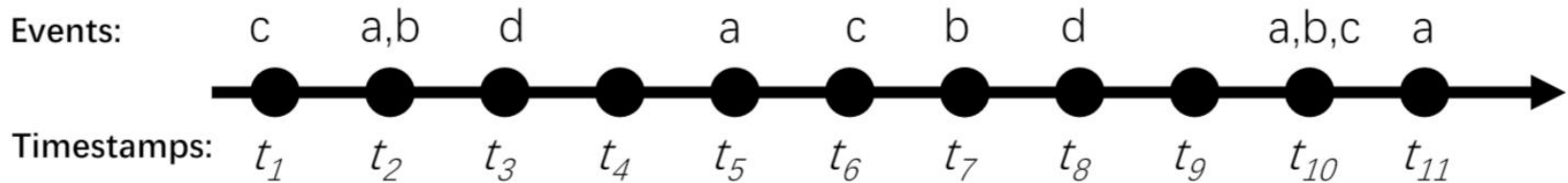
To address  
issues

## 2 Definitions



### Non redundant occurrences

---



For  $\text{Occ}(\{a, b, c\}) = \{[t_1, t_2], [t_5, t_7], [t_{10}, t_{10}]\}$ ,

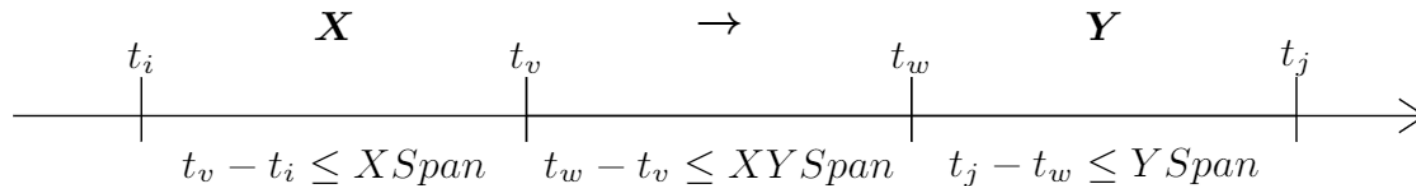
$[t_{10}, t_{11}]$  is overlapping with  $[t_{10}, t_{10}]$ , so  $[t_{10}, t_{11}]$  is redundant to  $\text{Occ}(\{a, b, c\})$

$\{[t_1, t_2], [t_5, t_7], [t_{10}, t_{10}]\}$ , is the set of non redundant occurrence of event set  $\{a, b, c\}$

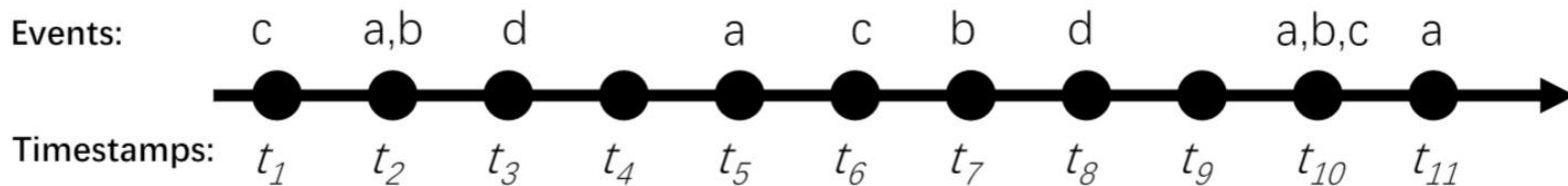
## 2 Definitions

### Partially-Ordered Episode Rules (POER)

$$X \rightarrow Y$$



For example:



minsup= 3, minconf= 0.6, XSpan= 3, XYSpan= 1, YSpan= 1

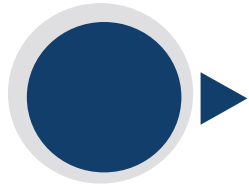
Occurrences of  $\{a, b, c\}$  are  $\text{Occ}(\{a, b, c\}) = \{[t_1, t_2], [t_5, t_7], [t_{10}, t_{10}]\}$

Occurrences of rule  $R: \{a, b, c\} \rightarrow \{d\}$  are  $\text{occ}(R) = \{[t_1, t_3], [t_5, t_8]\}$

Efficient algorithm: **POERM (ACIIDS 2021)**



## 2. Definitions

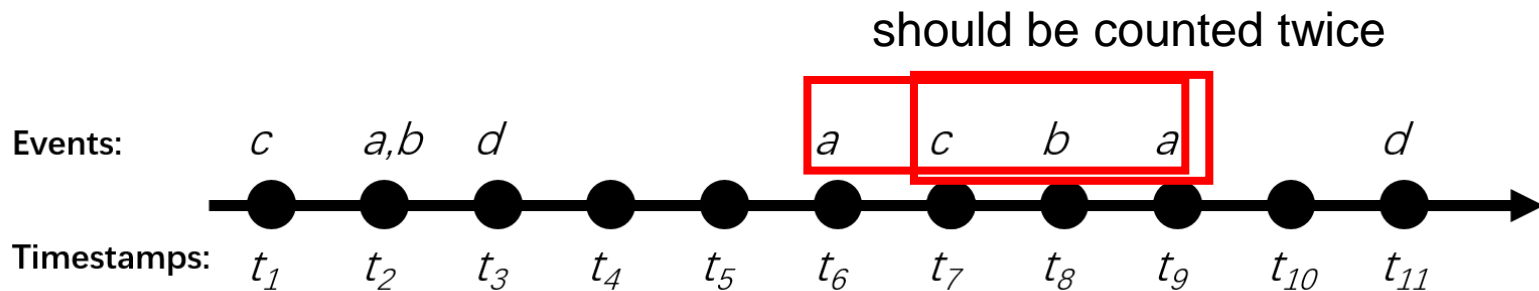
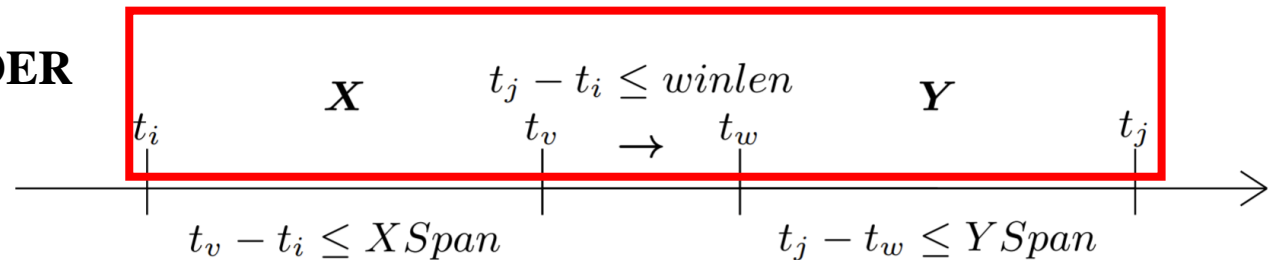


### POER with Head support

**Observation:** selecting POERs by counting their minimal occurrences can lead to undesirable results.

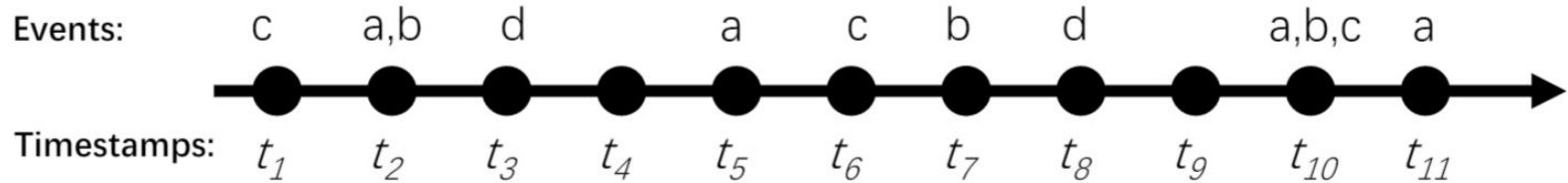
**Solution:** use the **Head Frequency** to calculate the support of POERs.

#### Head Frequency for POER





### 3. The POERMH algorithm



#### STEP 1: Find the frequent rule antecedents

minsup= 3



Frequent 1-event sets : {a} , {b}, {c}



extends i-event sets into i+1-event sets



Apply the quick sort algorithm to sort positions by ascending start point

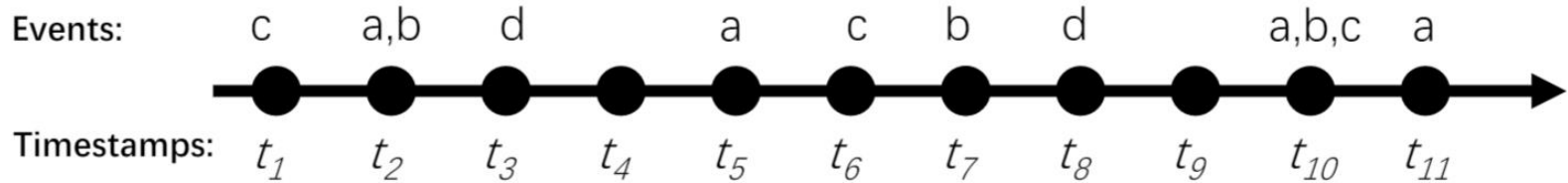


Count the Head Frequency and filter out the infrequent episodes





### 3. The POERMH algorithm



#### STEP 2: Find consequents to make rules

Frequent event sets :  $\langle \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}, \{a, b, c\} \rangle$

↓  
Frequent 1-event consequent rule

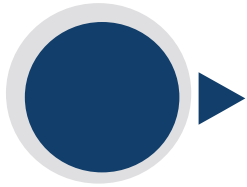
↓  
Extends i-event consequent rule into i+1-event consequent

↓  
For each occurrences  $[\text{pos.start}, \text{pos.end}]$  of i-event sets X

↓  
Search for  $[\text{pos.end} + 1, \text{winlen} - \text{pos.start}]$  to extend it

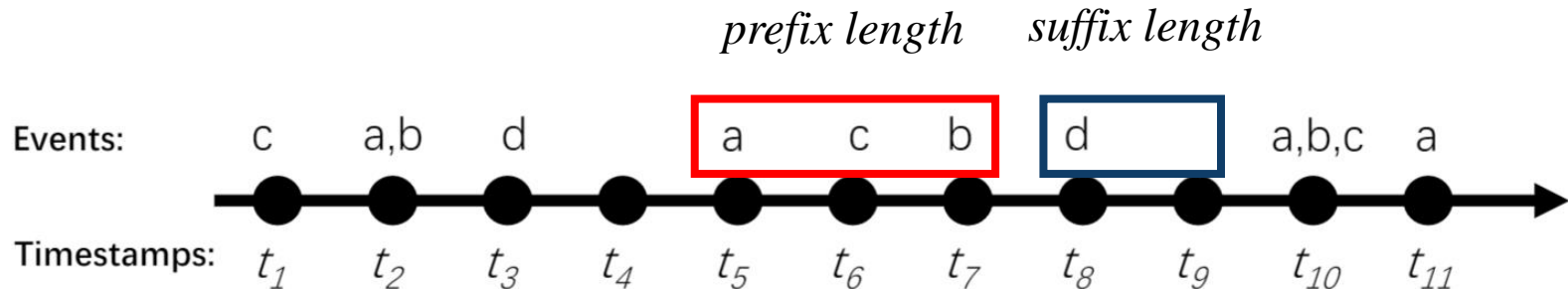


## 4. Experiment



### Sequence Prediction

**Task:** Predict an event that will appear in the suffix of a test sequence using the information from the prefix.



$$\text{accuracy} = \frac{\text{good predictions}}{\text{the number of prediction opportunities}}$$

$$\text{matching rate} = \frac{\text{good predictions} + \text{bad predictions}}{\text{the number of prediction opportunities}}$$



## 4 Experimental Evaluation

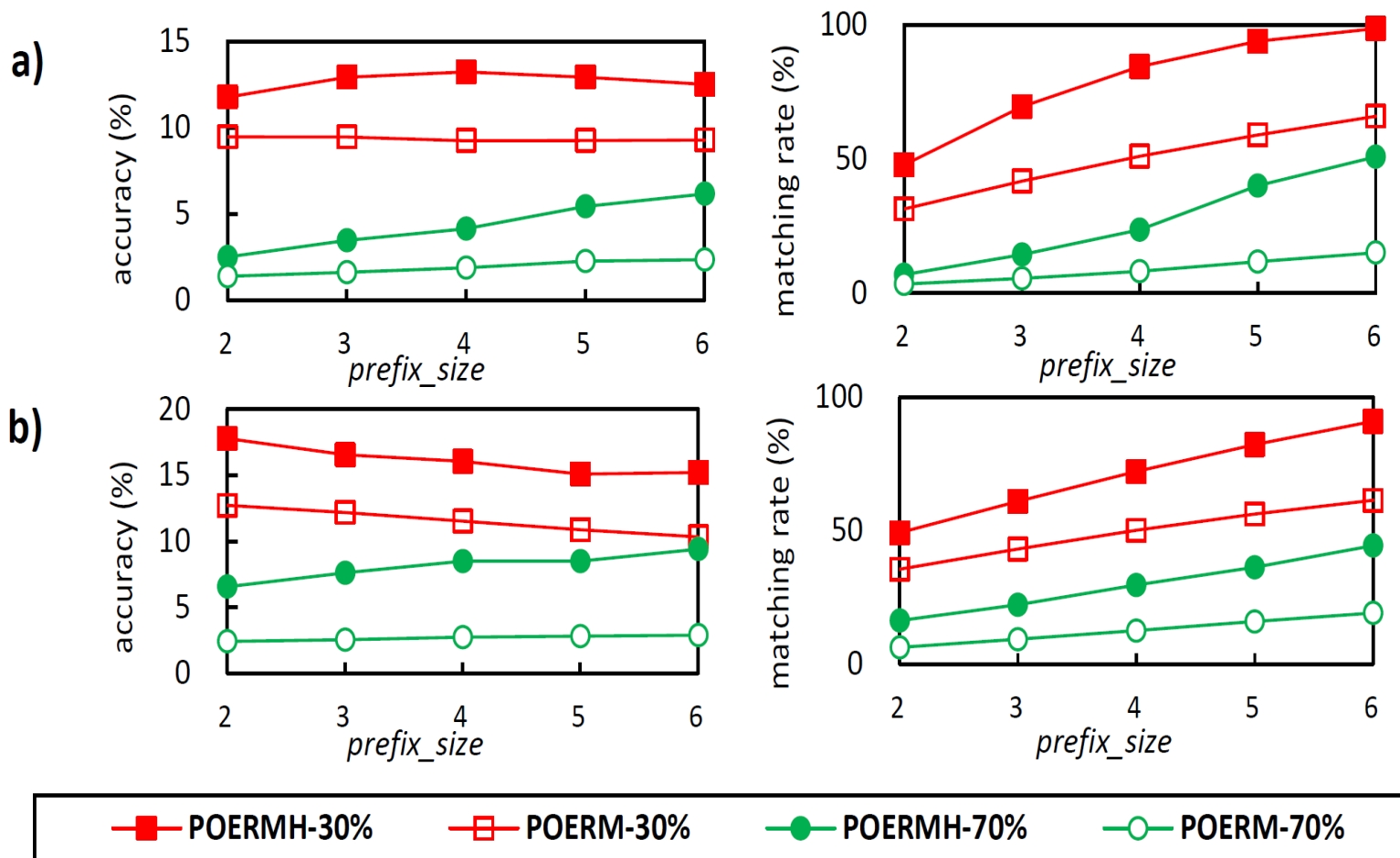
### Dataset and Default Values

Dataset	# Timestamps	# Events
Bible	649,024	13,905
Leviathan	153,682	9025

Default Values	minsup	minconf	suffixSize
Bible	120	0.3	1
Leviathan	80	0.3	2



## 4. Experimental Evaluation



**Observation:** POERM-H is more accurate and has a higher matching rate than POERM



## 5. Conclusion

### •Contributions:

- A new algorithm to find **partially-ordered episode rules** using the **head support**, named **POERMH**
- **Experiments** have shown that the POERMH has good sequence prediction performance compared to the benchmark **POERM** algorithm.

### •Future work:

- Consider adding optimizations to POERMH
  - Considering more complex data types
- **Open-source code, datasets:**
- [SPMF data mining library](#) (over 200 algorithms)

Thanks for listening!



# Our recent papers on episode rule mining:

- Chen, Y., Fournier-Viger, P., Nouioua, F., Wu, Y. (2021). **Mining Partially-Ordered Episode Rules with the Head Support**. Proc. 23rd Intern. Conf. on Data Warehousing and Knowledge Discovery (DAWAK 2021), Springer, LNCS, 7 pages **[POERMH algorithm]**
- Fournier-Viger, P., Chen, Y., Nouioua, F., Lin, J. C.-W. (2021). **Mining Partially-Ordered Episode Rules in an Event Sequence**. Proc. of the 13th Asian Conference on Intelligent Information and Database Systems ([ACIIDS 2021](#)), Springer LNAI, pp 3-15 **[POERM algorithm]**
- Chen, Y., Fournier-Viger, P., Nouioua, F., Wu, Y.. (2021). **Sequence Prediction using Partially-Ordered Episode Rules**. Proc. 4th International Workshop on Utility-Driven Mining (UDML 2021), in conjunction with the ICDM 2021 conference, IEEE ICDM workshop proceedings, to appear. **[POERM and POERMH for sequence prediction]**
- Ouarem, O., Nouioua, F., Fournier-Viger, P. (2021). **Mining Episode Rules From Event Sequences Under Non-Overlapping Frequency**. Proc. 34th Intern. Conf. on Industrial, Engineering and Other Applications of Applied Intelligent Systems (IEA AIE 2021), Springer LNAI, pp. 73-85. **[NONEPI algorithm]**